ON \mathcal{M} -HARMONIC SPACE \mathcal{B}_{n}^{s}

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Dedicated to the memory of Professor Slobodan Aljančić

Abstract. We give several characterizations of the Besov space \mathcal{B}_p^s of \mathcal{M} -harmonic functions in the open unit ball in \mathbb{C}^n .

1. Introduction and results

In [4] Hahn and Yousffi considered the boundary behavior in the Besov spaces \mathcal{B}_p^s of \mathcal{M} -harmonic functions in the open unit ball B in \mathbb{C}^n . In this paper we deal with several characterizations of the spaces \mathcal{B}_p^s . As a consequence we have:

- 1) If s > n, then $\mathcal{B}_p^s = \mathcal{A}_p^s$, where \mathcal{A}_p^s is the weighted Bergman space.
- 2) If s=n, the spaces \mathcal{B}_p^n are closely related to the Hardy spaces \mathcal{H}^p of \mathcal{M} -harmonic functions in B.
 - 3) For $0 \le s < n$, \mathcal{B}_p^s are Besov spaces (\mathcal{B}_p^0 is the diagonal Besov space).
- 4) For -p < s < 0 the functions in the space \mathcal{B}_p^s have Lipschitz continuity of order -s/p and thus extend continuously to the closed unit ball (see also Theorem 1.4 of [4]).
 - 5) If $s \leq -p$ then $\mathcal{B}_p^s = \{\text{constants}\}.$

Let $B=B_n$ be the open unit ball in \mathbb{C}^n and $S=\partial B$ the unit sphere in \mathbb{C}^n . We denote by ν the normalized Lebesgue measure on B and by σ the rotation invariant probability measure on S.

Let $\widetilde{\Delta}$ be the invariant Laplacian on B. That is, $\widetilde{\Delta}f(z) = \Delta(f \circ \varphi_z)(0)$, $f \in C^2(B)$, where Δ is the ordinary Laplacian and φ_z the standard automorphism of B, $\varphi_z \in \operatorname{Aut}(B)$, taking 0 to z (see [9]).

The C^2 -functions f that are an initiated by $\widetilde{\Delta}$ are called \mathcal{M} -harmonic $(f \in \mathcal{M})$.

Definition 1.1. For $0 , and <math>s \in \mathbb{R}$, the weighted Bergman space \mathcal{A}_p^s is defined as the space of \mathcal{M} -harmonic functions f on B for which

$$\|f\|_{\mathcal{A}^{s}_{p}} = \left[\int_{B} (1-|z|^{2})^{s} |f(z)|^{p} d\lambda(z)\right]^{1/p} < \infty,$$

where $d\lambda(z) = (1 - |z|^2)^{-n-1} d\nu(z)$ is the measure on B that is invariant under the group $\operatorname{Aut}(B)$.

For $f \in C^1(B)$, $Df = (\frac{\partial f}{\partial z_1}, \dots, \frac{\partial f}{\partial z_n})$, denotes the complex gradient of f, $\nabla f = (\frac{\partial f}{\partial x_1}, \dots, \frac{\partial f}{\partial x_{2n}})$, $z_k = x_{2k-1} + ix_{2k}$, $k = 1, 2, \dots, n$, denotes the real gradient of f.

For $f \in C^1(B)$ let $\widetilde{D}f(z) = D(f \circ \varphi_z)(0)$, $z \in B$, and $\widetilde{\nabla}f(z) = \nabla(f \circ \varphi_z)(0)$, $z \in B$, be the invariant complex gradient of f and the invariant real gradient of f respectively.

Definition 1.2. For $0 , and <math>s \in \mathbb{R}$, the \mathcal{M} -harmonic Dirishlet space \mathcal{D}_p^s is defined as the space of \mathcal{M} -harmonic functions f on B for which

$$\int_{B} |\widetilde{\nabla} f(z)|^{p} (1 - |z|^{2})^{s} d\lambda(z) < \infty.$$

The (differential) Bergman metric $b: B \times \mathbb{C}^n \mapsto \mathbb{R}$ is defined by

$$b(z,\xi) = \left(\frac{(1-|z|^2)|\xi|^2 + |\langle z,\xi\rangle|^2}{(1-|z|^2)^2}\right)^{1/2}.$$

For $f \in C^1(B)$, define the functional quantity

$$Qf(z) = \sup_{|\xi|=1} \frac{|\nabla f(z) \cdot \xi|}{b(z,\xi)} = \sup_{|\xi|=1} \frac{|\langle Df(z), \xi \rangle + \overline{\langle D\overline{f}(z), \xi \rangle}|}{b(z,\xi)}, z \in B.$$

This quantity is invariant under $\operatorname{Aut}(B)$, that is $Q(f \circ \varphi) = Q(f) \circ \varphi$, for all C^1 -functions f in B and $\varphi \in \operatorname{Aut}(B)$ (see $[\mathbf{5}, \mathbf{6}]$).

Definition 1.3. For $0 , <math>s \in \mathbb{R}$, let \mathcal{B}_p^s be the space of \mathcal{M} -harmonic functions f on B such that

$$||f||_{p,s} = \left(\int_B (Qf)^p(z)(1-|z|^2)^s d\lambda(z)\right)^{1/p} < \infty.$$

THEOREM 1.4. Let 0 , <math>s > n - p/2 and $f \in \mathcal{M}$. Then the following statements are equivalent:

(i)
$$f \in \mathcal{D}_p^s$$
, (ii) $f \in \mathcal{B}_p^s$, (iii) $\int_{R} |\nabla f(z)|^p (1 - |z|^2)^{s+p} d\lambda(z) < \infty$,

(iv)
$$\int_{R} (1-|z|^2)^{s+p} (|Rf(z)| + |\overline{R}f(z)|)^p d\lambda(z) < \infty.$$

As usual, $Rf(z) = \sum_{j=1}^{n} z_j \frac{\partial f}{\partial z_j}$, is the radial derivative of f and $\overline{R}f(z) = \sum_{j=1}^{n} \overline{z}_j \frac{\partial f}{\partial \overline{z}_j}$.

2. Proof of Theorem

If 0 < r < 1, we set $E_r(z) = \{w \in B : |\varphi_z(w)| < r\} = \varphi_z(rB)$. It is easy to see that $E_r(z)$ is an ellipsoid and its volume is given by $\nu(E_r(z)) = \frac{r^{2n}(1-|z|^2)^{n+1}}{(1-r|z|)^{n+1}}$ (see [9, p. 30]). We set $|E_r(z)| = \nu(E_r(z))$.

For the proof of Theorem 1.4 the following lemmas will be needed.

Lemma 2.1. [7] Let 0 < r < 1. There is a constanat C > 0 such that if $f \in \mathcal{M}$ then

(i)
$$|T_{ij}Rf(w)| \le C(1-|w|^2)^{-1/2} \int_{E_r(w)} |Rf(z)| d\lambda(z), \quad w \in B,$$

(ii)
$$|T_{ij}\overline{R}f(w)| \le C(1-|w|^2)^{-1/2} \int_{E_r(w)} |\overline{R}f(z)| d\lambda(z), \quad w \in B,$$

(ii)
$$|T_{ij}f(w)| \le C(1-|w|^2)^{-1/2} \int_{E_r(w)} |f(z)| d\lambda(z), \quad w \in B.$$

Here, as usual, $T_{ij} = \overline{z}_i \frac{\partial}{\partial z_j} - \overline{z}_j \frac{\partial}{\partial z_i}$, $\overline{T}_{ij} = z_i \frac{\partial}{\partial \overline{z}_j} - z_j \frac{\partial}{\partial \overline{z}_i}$, are tangential derivatives.

Here and elsewhere constants are denoted by C which may indicate a different constant from one occurrence to the next.

Lemma 2.2. If s > 1, then

$$\int_0^1 \frac{dt}{|1 - t \langle z, w \rangle|^s} \le \frac{C}{|1 - \langle z, w \rangle|^{s-1}}, \quad z, w \in B.$$

Lemma 2.3. [9, p. 17] If $\alpha > 0$, then

$$\int_{S} \frac{d\sigma(\xi)}{|1 - \langle \xi, z \rangle|^{n+\alpha}} = O\left(\frac{1}{(1 - |z|)^{\alpha}}\right), \quad z \in B.$$

It is easy to see that $|\widetilde{\nabla} f(z)| = Qf(z)$. Hence, $\mathcal{D}_p^s = \mathcal{B}_p^s$, for all $0 and <math>s \in \mathbb{R}$.

From the inequality $Qf(z) \ge (1-|z|^2)|\nabla f(z)|$ (see [4, p. 221]) it follows that (ii) \implies (iii).

(iii) \implies (iv) It is easy to see that if (iii) holds then

$$\int_{B} (1 - |z|^{2})^{s+p} \left| \frac{\partial f}{\partial z_{j}}(z) \right|^{p} d\lambda(z) < \infty, \ 1 \le j \le n,$$

$$\int_{B} (1 - |z|^{2})^{s+p} \left| \frac{\partial f}{\partial \overline{z}_{j}}(z) \right|^{p} d\lambda(z) < \infty, \ 1 \le j \le n,$$

which in turn implies that

$$\int_{B} (1 - |z|^{2})^{s+p} |Rf(z)|^{p} d\lambda(z) < \infty$$

$$\int_{B} (1 - |z|^{2})^{s+p} |\overline{R}f(z)|^{p} d\lambda(z) < \infty.$$

Thus, (iii) \implies (iv).

 $(iv) \implies (i)$ Assume now that

$$\int_{B} (1-|z|^{2})^{s+p} (|Rf(z)| + |\overline{R}f(z)|)^{p} d\lambda(z) < \infty.$$

It is easy to check that $|z|^2|Df(z)|^2=|Rf(z)|^2+\sum_{i< j}|T_{ij}f(z)|^2$. Using this and the equality

$$\begin{aligned} |\widetilde{\nabla}f(z)|^2 &= 2(|\widetilde{D}f(z)|^2 + |\widetilde{D}\overline{f}(z)|^2) \\ &= 2(1 - |z|^2)(|Df(z)|^2 - |Rf(z)|^2 + |D\overline{f}(z)|^2 - |R\overline{f}(z)|^2) \end{aligned}$$

(see [8]) we find that

$$|z|^{2}|\widetilde{\nabla}f(z)|^{2} = 2(1-|z|^{2})\left[(1-|z|^{2})(|Rf(z)|^{2}+|R\overline{f}(z)|^{2}) + \sum_{i < j} |T_{ij}f(z)|^{2} + \sum_{i < j} |T_{ij}\overline{f}(z)|^{2}\right].$$

Hence, to show that $f \in \mathcal{D}_p^s$ it is sufficient to show that

$$\int_{B} (1 - |z|^{2})^{s + p/2} (|T_{ij}f(z)|^{p} + |T_{ij}\overline{f}(z)|^{p}) d\lambda(z) < \infty, \ 1 \le i < j \le n.$$

Integration by parts shows that

$$f(z) = \int_0^1 \left[Rf(tz) + \overline{R}f(tz) + f(tz) \right] dt.$$

From this we conclude that it is sufficient to prove that

$$\int_{B} (1 - |z|^{2})^{s + p/2} \left(\int_{0}^{1} |T_{ij}u(tz)| dt \right)^{p} d\lambda(z) < \infty, \ 1 \le i < j \le n,$$

where u is Rf or $\overline{R}f$ or $R\overline{f}$ or $\overline{R}f$ or f.

We will show that, for fixed 1 < i < j < n,

$$I = \int_{B} (1 - |z|^2)^{s+p/2} \left(\int_{0}^{1} |T_{ij}Rf(tz)| dt \right)^{p} d\lambda(z) < \infty.$$

The remaining cases may be treated analogously.

Using Lemma 2.1, Fubini's theorem and Lemma 2.2 we find that for any a > 0

$$\begin{split} \int_{0}^{1} |T_{ij}Rf(tz)|dt &\leq C \int_{0}^{1} \left(\int_{E_{r}(tz)} \frac{|Rf(w)|(1-|w|^{2})^{a}}{|1-t\langle z,w\rangle|^{n+a+3/2}} d\nu(w) \right) dt \\ &\leq C \int_{0}^{1} \left(\int_{B} \frac{|Rf(w)|(1-|w|^{2})^{a} d\nu(w)}{|1-t\langle z,w\rangle|^{n+a+3/2}} \right) dt \\ &= C \int_{B} |Rf(w)|(1-|w|^{2})^{a} \left(\int_{0}^{1} \frac{dt}{|1-t\langle z,w\rangle|^{n+a+3/2}} \right) d\nu(w) \\ &\leq C \int_{B} \frac{|Rf(w)|(1-|w|^{2})^{a}}{|1-\langle z,w\rangle|^{n+a+1/2}} d\nu(w). \end{split}$$

Assume now 1 . Applying the continuous form of Minkowski's inequality we obtain

(2.1)
$$I \leq C \int_{0}^{1} (1-r)^{s+p/2-n-1} \cdot \left(\int_{0}^{1} \left(\int_{S} \left(\int_{S} \frac{|Rf(\rho\xi)|(1-\rho)^{a} d\sigma(\xi)}{|1-\langle r\zeta, \rho\xi \rangle|^{n+a+1/2}} \right)^{p} d\sigma(\zeta) \right)^{1/p} d\rho \right)^{p} dr.$$

By Hölder's inequality

$$\int_{S} \frac{|Rf(\rho\xi)|d\sigma(\xi)}{|1 - \langle r\zeta, \rho\xi \rangle|^{n+a+1/2}} \\
(2.2) \qquad \leq \left(\int_{S} \frac{|Rf(\rho\xi)|^{p}d\sigma(\xi)}{|1 - \langle r\zeta, \rho\xi \rangle|^{n+a+1/2}} \right)^{1/p} \left(\int_{S} \frac{d\sigma(\xi)}{|1 - \langle r\zeta, \rho\xi \rangle|^{n+a+1/2}} \right)^{1/p'} \\
\leq \frac{C}{(1 - r\rho)^{(a+1/2)/p'}} \left(\int_{S} \frac{|Rf(\rho\xi)|^{p}d\sigma(\xi)}{|1 - \langle r\zeta, \rho\xi \rangle|^{n+a+1/2}} \right)^{1/p}, \text{ by Lemma 2.3.} \\
(\text{Here } 1/p + 1/p' = 1).$$

Now we substitute (2.2) into (2.1) and use Fubini's theorem and Lemma 2.3 to get

$$I \leq C \int_{0}^{1} (1-r)^{s+p/2-n-1} \left(\int_{0}^{1} \frac{(1-\rho)^{a}}{(1-r\rho)^{(a+1/2)/p'}} \cdot \left(\int_{S} \left(\int_{S} \frac{|Rf(\rho\xi)|^{p} d\sigma(\xi)}{|1-\langle r\zeta, \rho\xi\rangle|^{n+a+1/2}} \right) d\sigma(\zeta) \right)^{1/p} d\rho \right)^{p} dr$$

$$= C \int_{0}^{1} (1-r)^{s+p/2-n-1} \left(\int_{0}^{1} \frac{(1-\rho)^{a}}{(1-r\rho)^{(a+1/2)/p'}} \cdot \left(\int_{S} |Rf(\rho\xi)|^{p} d\sigma(\xi) \int_{S} \frac{d\sigma(\zeta)}{|1-\langle r\zeta, \rho\xi\rangle|^{n+a+1/2}} \right)^{1/p} d\rho \right)^{p} dr$$

$$\leq C \int_{0}^{1} (1-r)^{s+p/2-n-1} \left(\int_{0}^{1} \frac{(1-\rho)^{a}}{(1-r\rho)^{a+1/2}} \cdot \left(\int_{S} |Rf(\rho\xi)|^{p} d\sigma(\xi) \right)^{1/p} d\rho \right)^{p} dr.$$

A simple observation shows that it is possible to select positive parameters a, t_1, t_2, t_3, t_4 such that

(i)
$$a = t_1 + t_2 = t_3 + t_4$$

(ii)
$$\frac{1}{p'} < t_3 - t_1 < \frac{s}{p} + \frac{3}{2} - \frac{n+1}{p}$$
, (iii) $t_2 > 1 + \frac{s}{p} - \frac{n+1}{p}$.

Note that here again we used the assumption that s > n - p/2.

Applying Hölder's inequality on (2.3) and Lemma 2.3 we obtain

$$\begin{split} I &\leq C \int_{0}^{1} (1-r)^{s+p/2-n-1} \left[\left(\int_{0}^{1} \frac{(1-\rho)^{t_1 p'} d\rho}{(1-r\rho)^{t_2 p'}} \right)^{p/p'} \\ & \cdot \left(\int_{0}^{1} \frac{(1-\rho)^{t_2 p}}{(1-r\rho)^{(t_4+1/2)p}} \left(\int_{S} |Rf(\rho\xi)|^p d\sigma(\xi) \right) d\rho \right) \right] dr \\ &\leq C \int_{0}^{1} (1-r)^{s+3p/2-n-2+(t_1-t_3)p} \left(\int_{0}^{1} \frac{(1-\rho)^{t_2 p}}{(1-r\rho)^{(t_4+1/2)p}} \right. \\ & \cdot \left(\int_{S} |Rf(\rho\xi)|^p d\sigma(\xi) \right) d\rho \right) dr \\ &= C \int_{0}^{1} \left[(1-\rho)^{t_2 p} \left(\int_{S} |Rf(\rho\xi)|^p d\sigma(\xi) \right) \left(\int_{0}^{1} \frac{(1-r)^{s+3p/2-n-2+(t_1-t_3)p} dr}{(1-r\rho)^{(t_4+1/2)p}} \right) \right] d\rho \\ &\leq C \int_{B} (1-|z|^2)^{s+p} |Rf(z)|^p d\nu(z) < \infty. \\ & \text{If } p=1 \text{, then} \\ &I \leq C \int_{B} (1-|z|^2)^{s+1/2} \left(\int_{B} \frac{|Rf(w)|(1-|w|^2)^a d\nu(w)}{|1-\langle z,w\rangle|^{n+a+1/2}} \right) d\lambda(z) \\ &\leq C \int_{0}^{1} (1-r)^{s+1/2-n-1} \left(\int_{0}^{1} (1-\rho)^a \left(\int_{S} |Rf(\rho\xi)| d\sigma(\xi) \right) d\rho \right) dr \\ &\leq C \int_{0}^{1} (1-r)^{s-n-1/2} \left(\int_{0}^{1} \frac{(1-\rho)^a}{(1-r\rho)^{a+1/2}} \left(\int_{S} |Rf(\rho\xi)| d\sigma(\xi) \right) d\rho \right) dr \\ &= C \int_{0}^{1} (1-\rho)^a \left(\int_{C} |Rf(\rho\xi)| d\sigma(\xi) \right) \left(\int_{0}^{1} \frac{(1-r)^{s-n-1/2}}{(1-r\rho)^{a+1/2}} dr \right) d\rho \end{split}$$

(We may assume that $a > \max\{s - n, 0\}$.)

For the case 0 the following lemma will be needed.

Lemma 2.4. Let 0 < r < 1 and 0 . There is a constant <math>C such that if $f \in \mathcal{M}$ then

$$(\mathrm{i}) \qquad \frac{|Rf(w)|^p}{|1-\langle z,w\rangle|^p} \leq C \int_{E_r(w)} \frac{|Rf(\xi)|^p}{|1-\langle z,\xi\rangle|^p} d\lambda(\xi), \; z,w \in B$$

 $\leq C \int_{\mathbb{R}} (1 - |w|^2)^{s-n} |Rf(w)| d\nu(w) < \infty.$

$$\text{(ii)} \qquad \left(\frac{|\overline{R}f(w)|}{|1-\langle z,w\rangle\,|}\right)^p \leq C\int_{E_r(w)} \left(\frac{|\overline{R}f(\xi)|}{|1-\langle z,\xi\rangle\,|}\right)^p d\lambda(\xi),\; z,w \in B$$

Note that the constant C is independent of z and w.

We will prove (i). The proof of (ii) is similar. By the formula (1.3) in [1]

$$Rf(w) = \int_S \frac{Rf(\varphi_w(\rho\xi))d\sigma(\xi)}{1 - \langle \rho\xi, w \rangle}, \ w \in B, \ 0 < \rho < 1.$$

Multiplying this equality by $2n\rho^{2n-1}(1-\rho^2)^{-n-1}h(\rho)d\rho$, where h is a radial function which belongs to $C^{\infty}(B)$ with compact support in B such that $\int_B h(z)d\lambda(z)=1$, then integrating from 0 to 1 and using the invariance of the measure λ , we get

$$Rf(w) = \int_{B} h(\varphi_{w}(z)) \frac{Rf(z)}{1 - \langle \varphi_{w}(z), w \rangle} d\lambda(z) = \int_{B} h(\varphi_{w}(z)) \frac{1 - \langle z, w \rangle}{1 - |w|^{2}} Rf(z) d\lambda(z)$$

by Theorem 2.2.5 [9, p. 28]. By a suitable choice of a function h we obtain

$$|Rf(w)| \le C \int_{E_r(w)} |Rf(\xi)| d\lambda(\xi), \ w \in B, \text{ for some } 0 < r < 1.$$

Since $|1 - \langle z, w \rangle| \simeq |1 - \langle z, \xi \rangle|$, if $\xi \in E_r(w)$, we have

$$\frac{|Rf(w)|}{|1-\langle z,w\rangle|} \leq C \int_{E_r(w)} \frac{|Rf(\xi)|}{|1-\langle z,\xi\rangle|} d\lambda(\xi),$$

and consequently,

$$\left(\frac{|Rf(w)|}{|1-\langle z,w\rangle\,|}\right)^p \leq C\int_{E_r(w)} \left(\frac{|Rf(\xi)|}{|1-\langle z,\xi\rangle\,|}\right)^p d\lambda(\xi), \ z,w \in B$$

(see [8]).

To finish the proof of Theorem 1.4 assume that 0 . Applying Theorem 3.2 (iii) [3] to the function

$$F(w) = \left(\frac{|Rf(w)|}{|1 - \langle z, w \rangle|^{a+n+1/2}}\right)^{p/2}, \quad w \in B \quad (z \in B \text{ - fixed})$$

and replacing p, r, k, q by 2, 2/p, 2/p, p(a+n+1) - n respectively and using Lemma 2.4 we find that

$$\left(\int_{B} \frac{|Rf(w)|(1-|w|^{2})^{a}d\nu(w)}{|1-\langle z,w\rangle\,|^{a+n+1/2}}\right)^{p} \leq C\int_{B} \frac{|Rf(w)|^{p}(1-|w|^{2})^{p(a+n+1)-n-1}d\nu(w)}{|1-\langle z,w\rangle\,|^{p(a+n+1/2)}}.$$

Thus, assuming that a > s/p - n,

$$\begin{split} I &\leq C \int_{B} (1-|z|^{2})^{s+p/2} \Biggl(\int_{B} \frac{|Rf(w)|^{p} (1-|w|^{2})^{p(a+n-1)-n-1} d\nu(w)}{|1-\langle z,w\rangle|^{p(a+n+1/2)}} \Biggr) d\lambda(z) \\ &= C \int_{B} |Rf(w)|^{p} (1-|w|^{2})^{p(a+n+1)-n-1} \Biggl(\int_{B} \frac{(1-|z|^{2})^{s+p/2-n-1} d\nu(z)}{|1-\langle z,w\rangle|^{p(a+n+1/2)}} \Biggr) d\nu(w) \\ &\leq C \int_{B} (1-|w|^{2})^{p+s} |Rf(w)|^{p} d\lambda(w) < \infty. \end{split}$$

This finishes the proof of Theorem 1.4.

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